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## Inversive congruential generator of the second order with a variable shift

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Our talk is devoted to research of statistical properties of the sequences of pseudorandom numbers produced by the inversive generator of second order

$$y_{n+1} \equiv \frac{a}{y_{n-1}y_n} + b + cF(n) \pmod{p^m}, \quad (1)$$

with  $(a, p) = (y_0, p) = (y_1, p) = 1$ ,  $b \equiv c \equiv 0 \pmod{p}$ , and  $F(n) \in \mathbb{Z}[n]$ .

Using the recursion (1) we obtain the representation

$$y_n = \frac{A_0^{(n)} + A_1^{(n)}y_0 + A_2^{(n)}y_1 + A_3^{(n)}y_0y_1}{B_0^{(n)} + B_1^{(n)}y_0 + B_2^{(n)}y_1 + B_3^{(n)}y_0y_1}, \quad (2)$$

where the coefficients  $A_j^{(n)}$ ,  $B_j^{(n)}$ ,  $j = 0, 1, 2, 3$  can be prescribe as the polynomials  $f_i(k)$  for  $n = 3k + i$ ,  $i = 0, 1, 2$ .

We determinate a period length of the sequence  $\{y_n\}$ , besides this period reaches a maximum  $\tau = 3p^{m-\nu_0-\alpha}$  if  $\nu_p(y_0y_1^2 - a) < \nu_p(b) = \alpha$ .

Moreover, we prove that the sequence of pseudorandom numbers passes 3-dimensional test on the statistical independence. Obtained results are analogue of similar results for the congruential inversive pseudorandom sequences of the first order investigated in [1],[2].

### References

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2. S. Varbanets, *Generalizations of Inversive Congruential Generator. Analytic and Probabilistic Methods in Number Theory*, Proceedings of the Fifth International Conference in Honour of J. Kubilius, Palanga, Lithuania, 4-10 September 2011, 2012. P. 265-282.

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